



# Mathematics and Problem Solving

Lecture 10.1

Statistics

# Statistics

- A **statistic** is a number that provides a summary of a set of other numbers
  - Statistics are key to modern science
  - Most modern AI is essentially sophisticated statistics

# A simple statistic

- Lets say you have some text that has been encrypted using a simple cipher. It looks something like this:
  - rhy iuksq plcaz bcd nuwfo cxyl rhy tmjg  
vce
- We can **count** each letter
  - In English, 'e' is more common than 'q'.

# Numeric Data

- Often our data takes the form of numbers
  - 1, 4, 2.2, 5.3, 8.2, 2.1, ... etc.
- i.e. **numeric** or **ratio** or **scalar data**
  - Temperature measurements
  - Game scores
- **Can be ordered**, and the **differences between values** is meaningful

# Ordinal Data

- **Ordinal data** can be **ordered**, but the **ratio** between the values is not meaningful
- e.g. we ask people to rate how much they enjoyed using our app, on a scale of 1-5
  - 1, 2, 5, 2, 3, 4, 1, 2
  - In this case 2 does not necessarily mean they enjoyed it twice as much as 1

# Nominal Data

- **Nominal data** has no natural ordering
- e.g. we ask 6 people for their favourite animal
  - Cat, Dog, Squirrel, Dog, Dog, Rabbit

# Statistics

- There are two types of statistics
  - **Descriptive Statistics**
    - Describe properties of your data (e.g. counting occurrences)
  - **Inferential Statistics**
    - Used to infer things about the world from data. (e.g. hypothesis testing)

# Applying Descriptive Statistics

- Lets say you're designing a game that involves probability (e.g. rolling dice)
- There are three ways to analyse it
  - Playtesting
  - Analytically
  - Statistically – through simulation



# Applying Inferential Statistics

- **A/B testing** is widespread online
  - Deliver a new version of a website/game to a subset of users
  - Measure something (click throughs, conversions, etc.)
  - Compare the test population against a control group to determine whether the change improved engagement (**hypothesis testing**)

# Variables

- **Independent Variable** (IV)
  - The thing you control
- **Dependant Variable** (DV)
  - The thing that you observe

# Summary

- Statistics are useful
  - Describe what things are like
  - Test links between things
- What type of data do you have?
  - Nominal
  - Ordinal
  - Numeric